

SEAMLESS PHASE II/III CLINICAL TRIALS WITH COVARIATE ADAPTIVE RANDOMIZATION

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Abstract: There is an urgent need to evaluate new therapies in a time-sensitive and cost-effective manner. We propose the adaptive seamless phase II/III clinical trials with covariate adaptive randomization (CAR) to satisfy this need. CAR is one of the most popular designs in randomized controlled trials, enhancing covariance balance and ensuring valid treatment comparisons. However, it has several challenges: (1) the type I error rate of the commonly used Student's t -test following CAR can be inflated because of the seamless trials, but can also be decreased using CAR; (2) the complicated allocation mechanism induced by CAR causes extra difficulties to derive the asymptotic properties of a test procedure; and (3) previous theoretical studies of seamless trials rely mainly on the assumption of complete randomization, a procedure rarely used in real trials. We establish a theoretical foundation for adaptive seamless phase II/III trials with CAR. We also propose an approach that is easy to implement in order to control the type I error rate and improve the power when using Student's t -test. This important step will promote the application of this procedure.

Key words and phrases: Adaptive design, type I error, power.

1. Introduction

In 2006, the US Food and Drug Administration (FDA) emphasized the importance of streamlining clinical trials (US FDA (2006)). Since then, there has been an urgent need to evaluate new therapies in a time-sensitive and cost-effective manner without compromising the integrity and validity of the development process. In this paper, we propose the adaptive seamless phase II/III clinical trials with covariate adaptive randomization (CAR) to satisfy this need. Recently, the FDA drafted guidance on seamless clinical trials, aiming to broaden acceptance of the design (US FDA (2018)). CAR is one of the most popular clinical trial designs. It ensures valid treatment comparisons by balancing potentially confounding patient characteristics across the treatment arms. We establish a

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theoretical foundation for adaptive seamless phase II/III trials with CAR in order to facilitate the application of this design in practice. We address three major challenges: the theoretical properties of this complicated allocation and analysis procedure; control of the type I error rate; and improvement of the power.

In a typical seamless phase II/III clinical trial (Thall, Simon and Ellenberg (1988); Jennison and Turnbull (2007); Hampson and Jennison (2015)), multiple experimental treatments or drug doses are simultaneously compared against a control in the phase II trial; the candidates with the best performance are then selected for the phase III trial; and an analysis based on data from both phases is performed at the end of the trial. By using a single protocol for the two phases, the seamless design avoids the lead time between conventional phase II and phase III trials, which is likely to be six months or more. It also reduces the number of trials required to compare multiple drugs, decreases the sample size, and allows longer monitoring of the patients from phase II (Bretz et al. (2009)). These advantages increase the profits of pharmaceutical companies and have received much attention from industry. By 2016, more than 40 active, first-in-human cancer trials had used the seamless strategy (Prowell, Theoret and Pazdur (2016)). An example highlighted by Bhatt and Mehta (2016) is the Indacaterol to Help Achieve New COPD Treatment Excellence (INHANCE) trial Barnes et al. (2010), a seamless phase II/III clinical trial of inhaled indacaterol for the treatment of chronic obstructive pulmonary disease (COPD) using an equal allocation with stratification for smoker status.

For seamless clinical trials, it is critical to control the possibly inflated type I error rate under the dual influence of multiplicity and selection (Bauer et al. (2010)). Following the approach of Bauer and Kieser (1999), Bretz et al. (2006) and Schmidli et al. (2006) used the closure principle (Marcus, Eric and Gabriel (1976)), combination tests (Bauer and Köhne (1994); Lehmacher and Wassmer (1999)), and multiple testing procedures (Simes (1986); Dunnett (1955)) to control the familywise type I error rate. Liu, Proschan and Pledger (2002) provided a solid theoretical foundation for general two-stage adaptive designs. Koenig et al. (2008) proposed the adaptive Dunnett test based on the conditional error rate (Müller and Schäfer (2001)). However, the theory of most of these studies assume complete randomization with independent responses, which is rarely applied in clinical trials, and these approaches may not be valid under other randomization schemes.

It is well known that an imbalance of the confounding covariates across treatments may bias the study results. This imbalance can be mitigated by CAR that sequentially assigns the next patient based on the previous treatment assign-

ments and covariates, as well as on the current covariate profile. CAR can also reduce the selection bias, minimize the accidental bias, and improve the statistical efficiency (Shao, Yu and Zhong (2010)). The most commonly used CAR in randomized controlled trials is the stratified permuted block (SPB) design. Other CAR designs and clinical trials adopting CAR include those of Pocock and Simon (1975), Antognini and Zagoraiou (2011), Iacono et al. (2006), Jakob et al. (2012), and Krueger et al. (2007), as well as Barnes et al. (2010) mentioned above, a seamless phase II/III trial with CAR.

In practice, unadjusted analyses, such as Student's t -test, are commonly used in clinical trials (Kahan et al. (2014); Sverdlov (2015)). This simple approach avoids a model misspecification, but results in a conservative type I error rate under CAR (Shao, Yu and Zhong (2010)). Hypothesis testing and sequential monitoring in clinical trials with CAR have recently been studied by Shao, Yu and Zhong (2010), Ma, Hu and Zhang (2015), Bugni, Canay and Shaikh (2018), and Zhu and Hu (2019). However, none of these studies investigated the application of CAR in seamless phase II/III trials.

Seamless phase II/III designs and CAR with Student's t -test both lead to difficulties in controlling the type I error rate. It is challenging to perform the theoretical investigation and propose approaches to control the type I error rate for seamless phase II/III trials with CAR, for several reasons: (1) the correlation structure of the within-stratum imbalances is complex; (2) the relationships among the treatment assignments, covariates, and responses are complicated; (3) the allocation functions are discrete; and (4) the data used in the treatment selection are also used for inference at the end of the trial. Therefore, seamless phase II/III clinical trials with CAR currently lack a theoretical foundation, and control of the type I error rate is based on the assumption of complete randomization.

In this paper, we provide a theoretical foundation for seamless phase II/III clinical trials with CAR. We also propose ways to adjust the Student's t -test statistics and use the test procedures available for complete randomization to control the type I error rate and improve the power. This provides clinical trial practitioners with valid tests and treatment comparisons in seamless clinical trials with CAR. We also investigate estimation and hypothesis testing for CAR with multiple treatments, which has a crucial implication for a single phase with multiple treatments. Our numerical studies show that, compared with traditional methods, our procedure controls the type I error rate well and increases the power significantly.

2. Seamless Phase II/III Clinical Trials with CAR

2.1. Framework of seamless phase II/III clinical trials

We consider a seamless phase II/III trial and refer to the two phases as Stage 1 and Stage 2, respectively. Assume the planned sample size for Stage 1 is N , and the planned sample size for Stage 2 is N' , so the total sample size is $N + N'$. The *design procedure* is described below.

Stage 1. The first N patients are sequentially assigned to K experimental treatments and the control arm with CAR. One treatment, say treatment k^* , is then chosen for Stage 2 based on certain criteria, for example, the one with the largest estimated treatment effect and an acceptable safety profile.

Stage 2. The remaining N' patients are sequentially assigned to treatment k^* and the control arm with CAR. A final analysis comparing treatment k^* and the control arm is performed using the data from both stages.

We next describe the *analysis procedure* with a flowchart in Figure 1.

Let $\boldsymbol{\mu} = (\mu_0, \mu_1, \dots, \mu_K)^\top$ denote the vector of treatment effects, with μ_0 corresponding to the control arm, and μ_k , for $k = 1, \dots, K$, corresponding to K experimental treatments. At the end of the trial, without loss of generality, we test $H_{0,k^*} : \mu_{k^*} = \mu_0$ versus $H_{1,k^*} : \mu_{k^*} > \mu_0$ based on the combined data from the two stages, using the closure principle (Marcus, Eric and Gabriel (1976)) to control the familywise type I error rate. The closure principle rejects H_{0,k^*} at level α if each intersection hypothesis $H_{0,I}$, with $k^* \in I, I \subseteq \{1, \dots, K\}$, is rejected at level α , where $H_{0,I} = \bigcap_{k \in I} H_{0,k}$, with $H_{0,k} : \mu_k = \mu_0$.

To test each intersection hypothesis $H_{0,I}$ using the data from the two stages, we use a combination test such as the inverse χ^2 method (Bauer and Köhne (1994)). Let $P_{1,I}$ and $P_{2,I}$ denote the p -values for $H_{0,I}$ based on the data from Stage 1 and Stage 2, respectively. Then the inverse χ^2 method rejects $H_{0,I}$ if $-\log(P_{1,I}P_{2,I}) > \chi_4^2(1 - \alpha)/2$, where $\chi_4^2(1 - \alpha)$ is the $(1 - \alpha)$ th quantile of the χ^2 distribution with four degrees of freedom. An alternative approach is the weighted inverse normal method (Lehmacher and Wassmer (1999)).

To perform the combination test, we calculate the adjusted p -values for each stage, $P_{1,I}$ and $P_{2,I}$, using either the Simes test or the Dunnett test. Note that both tests reduce to the usual Student's t -test if there is only one treatment and one control arm, as in Stage 2. We now briefly review the Simes test and the Dunnett test when they are used under complete randomization, deferring the justification and modification of these methods under CAR to Section 2.3. We illustrate the test procedures for Stage 1 using multiple treatments because the

Stage 2 comparison between two arms is straightforward.

Suppose the intersection hypothesis $H_{0,I}$ is composed of m elementary hypotheses $H_{0,k}$, with the associated p -values denoted by $P_{1,k}$. Let $P_{1,(j)}$, for $j = 1, \dots, m$, be the p -values in ascending order. Using the Simes test, we have the adjusted p -value $P_{1,I} = \min_{1 \leq j \leq m} (mP_{1,(j)}/j)$ for the intersection hypothesis $H_{0,I}$.

For the Dunnett test, without loss of generality, consider $H_{0,I}$ with $I = \{1, \dots, K\}$. Let

$$t_k = \frac{\bar{Y}_k - \bar{Y}_0}{s(1/N_k + 1/N_0)^{1/2}}, \quad k = 1, \dots, K, \quad (2.1)$$

where N_k is the number of patients assigned to treatment k ; \bar{Y}_k and S_k^2 are the sample mean and sample variance, respectively, under treatment k ; and $s^2 = \sum_{k=0}^K (N_k - 1)S_k^2/\nu$, with $\nu = N - K - 1$. Under complete randomization, the null distribution of $(t_1, \dots, t_K)^T$ is the K -variate t -distribution with ν degrees of freedom and correlations

$$\rho_{k,k'} = \left(\frac{N_k}{N_k + N_0} \right)^{1/2} \left(\frac{N_{k'}}{N_{k'} + N_0} \right)^{1/2}, \quad k, k' = 1, \dots, K.$$

Then, the conventional Dunnett test rejects the intersection hypothesis $H_{0,I}$ at level α if

$$\max_{1 \leq k \leq K} t_k \geq c,$$

where c is determined by $\text{pr}(\zeta_1 < c, \dots, \zeta_K < c) = 1 - \alpha$, and $(\zeta_1, \dots, \zeta_K)^T$ follows the K -variate t -distribution with ν degrees of freedom and correlations $\rho_{k,k'}$.

In the literature, the above analysis procedure is used in seamless trials to control the familywise type I error rate, with the assumption that patients are allocated using complete randomization and the responses of the patients are independent of each other. However, the responses and treatment assignments are no longer independent under CAR, because of the complicated randomization mechanism that balances the covariates over different arms. When there are two arms in a phase III clinical trial, the conventional tests are too conservative with a small type I error rate because of CAR (Shao, Yu and Zhong (2010); Ma, Hu and Zhang (2015)). It is unclear whether CAR will lead to a conservative type I error rate in seamless clinical trials, and it is worth investigating the underlying theory. Based on the closure principle (Marcus, Eric and Gabriel (1976)) and the conditional invariance principle (Brannath, Koenig and Bauer (2007); Brannath, Gutjahr and Bauer (2012)), for a valid treatment comparison,

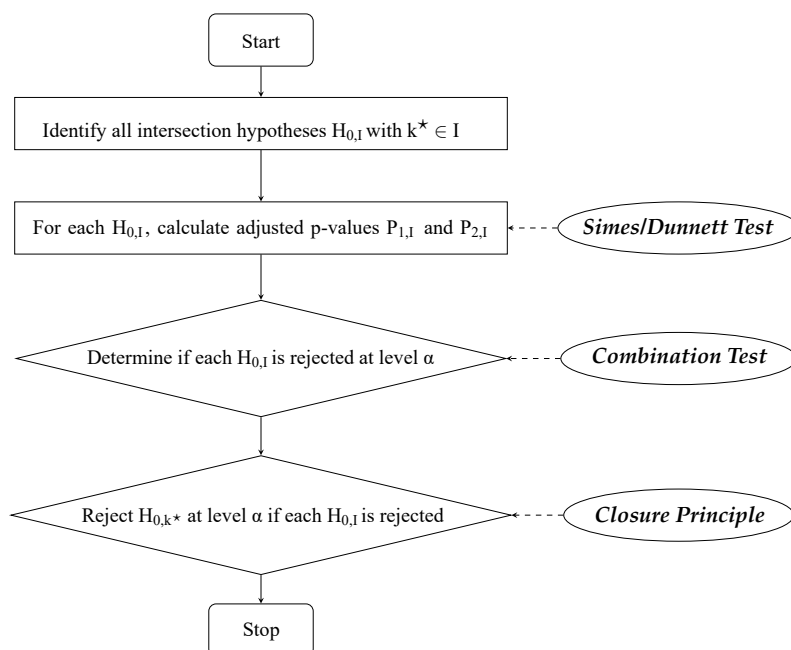


Figure 1. Flowchart of the analysis procedure of testing H_{0,k^*} .

it suffices to validate the Simes test and the Dunnett test under CAR for each stage of the above design and analysis procedure.

2.2. Estimation following CAR with multiple treatments

In this section, we study the estimation for CAR with multiple treatments, a key element for an adaptive seamless II/III trial and an important problem in its own right, with implications for a traditional single-phase clinical trial with CAR and multiple treatments.

Suppose a CAR procedure is implemented to assign the patients to $(K + 1)$ arms, and the total sample size is N . Let Z_i , for $i = 1, \dots, N$, represent the covariate information for the i th patient. We allow Z_i to be either discrete or continuous covariates and assume that the covariates are all independent and identically distributed (i.i.d.). To incorporate continuous covariates into the randomization procedure, we discretize Z_i using $D(Z_i)$, a discrete function of Z_i taking values in a finite set \mathcal{D} . We can set $D(Z_i) = Z_i$ for discrete covariates, so both types of covariates can be treated using the same notation. For simplicity, we introduce our methods using the univariate covariate Z_i with variance σ_z^2 ; the conclusions can be extended easily to multivariate cases.

Let $\mathbf{T}_i = (T_{i0}, T_{i1}, \dots, T_{iK})^\top$ indicate the treatment assignment for the i th patient, where treatment 0 represents the control arm. We have $T_{ik} = 1$, for $k = 0, 1, \dots, K$, if the i th patient is assigned to treatment k , and $T_{ik} = 0$ otherwise. Then, $N_k = \sum_{i=1}^N T_{ik}$, for $k = 0, 1, \dots, K$, is the number of patients in treatment k after N patients have been assigned. Let $\mathbf{Y}_i = (Y_{i0}, Y_{i1}, \dots, Y_{iK})^\top$, for $i = 1, \dots, N$, be a random vector of response variables, where Y_{ik} , for $k = 0, 1, \dots, K$, is the response of the i th patient under treatment k . Only one element of \mathbf{Y}_i , say Y_{ik} , can be observed if $T_{ik} = 1$. Assume the response of the i th patient under treatment k follows

$$Y_{ik} = \mu_k + \beta Z_i + \varepsilon_{ik}, \quad i = 1, \dots, N,$$

where β represents the covariate effect, and ε_{ik} s are i.i.d random errors with mean zero and constant variance σ_ε^2 and are independent of the covariates. In practice, to avoid unnecessary or incorrect model assumptions, a natural treatment effect estimator for treatment k , for $k = 0, 1, \dots, K$, is $\bar{Y}_k = \sum_{i=1}^N T_{ik} Y_{ik} / N_k$.

We first introduce two conditions for the balancing properties under CAR with multiple treatments. For any $k = 1, \dots, K$:

Condition 1. $N_k - N_0 = O_p(1)$.

Condition 2. $\sum_{i=1}^N (T_{ik} - T_{i0}) I\{D(Z_i) = d\} = O_p(1)$ for any $d \in \mathcal{D}$.

These two conditions ensure that good balancing properties are attained under a CAR procedure. Condition (A) indicates that the number of patients in each treatment group is approximately equal, and Condition (B) implies a balance of treatment assignments within each covariate stratum formed by $D(Z_i)$. Both conditions are satisfied by the stratified permuted block design with multiple treatments. Note that Condition (B) implies Condition (A) when the number of stratum is finite. We list both conditions to emphasize the balancing properties with respect to different levels (overall and within-stratum), similarly to Ma, Hu and Zhang (2015).

Remark 1. The two conditions can be considered a generalization of those used in Shao, Yu and Zhong (2010) and Ma, Hu and Zhang (2015), where only two arms (one treatment and one control) are considered.

Now, we present our theorem on the treatment effect estimation. We write $\mathbf{1}$ for a column vector of ones, with a subscript denoting its dimension.

Theorem 1. *Under Conditions (A) and (B), as $N \rightarrow \infty$,*

$$\left(\frac{N}{K+1}\right)^{1/2} \left\{ (\bar{Y}_0, \bar{Y}_1, \dots, \bar{Y}_K)^\top - (\mu_0, \mu_1, \dots, \mu_K)^\top \right\}$$

converges in distribution to a normal distribution with mean zero and covariance matrix \mathbf{V} , where $\mathbf{V} = \text{diag}\{\sigma_d^2 \mathbf{1}_{K+1}\} + (K+1)^{-1} \beta^2 \text{Var}[E\{Z_i \mid D(Z_i)\}] \mathbf{1}_{K+1} \mathbf{1}_{K+1}^\top$ and $\sigma_d^2 = \sigma_\varepsilon^2 + \beta^2 E[\text{Var}\{Z_i \mid D(Z_i)\}]$.

The theorem gives the asymptotic distribution of the average responses of different treatment groups. It is clear that these treatment effect estimators are no longer independent and are positively correlated, which is a key difference compared with complete randomization. The dependence structure arises from the randomization procedure that adaptively assigns patients to the treatment arms to enhance the covariate balance.

Remark 2. Under complete randomization, the asymptotic covariance matrix of $\{N/(K+1)\}^{1/2}(\bar{Y}_0, \bar{Y}_1, \dots, \bar{Y}_K)^\top$ is a diagonal matrix with the diagonal entries equal to $\sigma_\varepsilon^2 + \beta^2 \sigma_Z^2$, which is larger than $\sigma_d^2 + (K+1)^{-1} \beta^2 \text{Var}[E\{Z_i \mid D(Z_i)\}]$ under CAR. Thus, CAR can increase the precision of the estimation of the mean response of each treatment group by balancing the covariates.

The theorem can be used to study the properties of any linear transformation of $(\bar{Y}_0, \bar{Y}_1, \dots, \bar{Y}_K)^\top$. However, our main interest is in comparing the treatment effects between the experimental treatments and the control. The next corollary is a direct consequence of Theorem 1 and provides the asymptotic joint distribution of $\bar{Y}_k - \bar{Y}_0$, for $k = 1, \dots, K$.

Corollary 1. *Under Conditions (A) and (B), as $N \rightarrow \infty$,*

$$\left(\frac{N}{K+1}\right)^{1/2} \left\{ (\bar{Y}_1 - \bar{Y}_0, \dots, \bar{Y}_K - \bar{Y}_0)^\top - (\mu_1 - \mu_0, \dots, \mu_K - \mu_0)^\top \right\}$$

converges in distribution to a normal distribution with mean zero and covariance matrix Σ , where $\Sigma = \text{diag}\{\sigma_d^2 \mathbf{1}_K\} + \sigma_d^2 \mathbf{1}_K \mathbf{1}_K^\top$.

Corollary 1 reveals that the asymptotic variance of $\bar{Y}_k - \bar{Y}_0$ under CAR is smaller than that under complete randomization. In particular, when Z_i are discrete covariates, the asymptotic variance of $\{N/(K+1)\}^{1/2}(\bar{Y}_k - \bar{Y}_0)$ is $2\sigma_\varepsilon^2$, compared to $2(\sigma_\varepsilon^2 + \beta^2 \sigma_z^2)$ under complete randomization. This can be interpreted to mean that the covariates are balanced so well that the variability of the difference in means between the two groups is due only to the random errors. The corollary provides a theoretical foundation for deriving a valid test with a correct type I error rate.

2.3. Control of type I error rate in seamless clinical trials with CAR

The commonly used test statistic for $H_{0,k} : \mu_k = \mu_0$ is based on a form of $\bar{Y}_k - \bar{Y}_0$ that is normalized to have a unit variance. The next theorem follows Theorem 1 and shows how to construct such test statistics.

Theorem 2. *Assume that Conditions (A) and (B) hold. Let*

$$X_k = \frac{\bar{Y}_k - \bar{Y}_0}{\sigma_d(1/N_k + 1/N_0)^{1/2}}, \quad k = 1, \dots, K.$$

If the null hypotheses $H_{0,k} : \mu_k = \mu_0$ are true for all $k = 1, \dots, K$, then, as $N \rightarrow \infty$, $(X_1, \dots, X_K)^T$ converges in distribution to a normal distribution with mean zero and covariance matrix \mathbf{R} , where $\mathbf{R} = \text{diag}\{\mathbf{1}_K/2\} + \mathbf{1}_K\mathbf{1}_K^T/2$.

Based on Theorem 2, X_k following a standard normal distribution can be used as the test statistic to test the individual null hypothesis $H_{0,k} : \mu_k = \mu_0$, and the critical value can be selected accordingly. Note that the asymptotic distribution remains unchanged if σ_d is replaced by its consistent estimator $\hat{\sigma}_d$, which is usually obtained in practice using either the model-based method or the bootstrap method. We propose fitting a linear regression using all of the stratification covariates in the model to obtain consistent estimators for the parameters in the expression of σ_d in Theorem 1 and to calculate the estimate of σ_d accordingly. By the continuous mapping theorem, $\hat{\sigma}_d$ obtained in this way is a consistent estimator of σ_d . We illustrate these methods in Section 3.

Remark 3. Compared with t_k defined in (2.1) that is valid under complete randomization, we find that σ_d or its consistent estimator must be used instead of s to construct the test statistics under CAR. Otherwise, the asymptotic distribution is more concentrated around zero than the standard normal distribution, and the actual type I error rates are smaller than the nominal levels.

As argued previously, to control the type I error rate for seamless phase II/III clinical trials, it is critical and sufficient to prove that the Simes test or the Dunnett test is still valid with the test statistics X_k under CAR. In Theorem 2, we have successfully detected that the joint distribution of $(X_1, \dots, X_K)^T$ is an equicorrelated multivariate normal distribution with a nonnegative correlation. The following theorem is an immediate consequence of Result 1 in Sarkar and Chang (1997).

Theorem 3. *Under Conditions (A) and (B), the type I error rate is controlled for the Simes test with the test statistics X_k , for $k = 1, \dots, K$, under CAR.*

We next consider the Dunnett test. In Theorem 2, we proved that the vector of test statistics $(X_1, \dots, X_K)^\top$ asymptotically follows a K -dimensional normal distribution with unit variances and constant correlations equal to $1/2$. To obtain a valid test, we can reject the null hypotheses if

$$\max_{1 \leq k \leq K} X_k \geq c', \quad (2.2)$$

where c' is determined by $\text{pr}(\xi_1 < c', \dots, \xi_K < c') = 1 - \alpha$, and $(\xi_1, \dots, \xi_K)^\top$ follows the normal distribution $\mathcal{N}(\mathbf{0}, \mathbf{R})$. Note that the test considered here is based on X_k defined in Theorem 2 instead of the conventional t_k used under complete randomization. In addition, the original Dunnett test is based on the multivariate t distribution, whereas the test presented here uses the normal distribution, which relies on the asymptotic normality given in Theorem 2. For these reasons, we refer to the test based on X_k and rejection region (2.2) as the modified Dunnett test, although we call it the Dunnett test for simplicity when there is no confusion.

An application of Theorem 2 yields the following theorem.

Theorem 4. *Under Conditions (A) and (B), the type I error rate is asymptotically α for the Dunnett test with test statistics X_k , for $k = 1, \dots, K$, under CAR.*

Theorems 3 and 4 show that the widely used Simes and Dunnett tests can also be applied under CAR, provided an appropriate adjustment is made to the test statistics. Combined with the results from the last section, the design and analysis procedures for seamless phase II/III clinical trials with CAR (described in Section 2.1) can lead to higher precision and valid inferences for treatment effects, showing the advantages of balancing the covariates over complete randomization.

3. Numerical Studies

We have obtained the asymptotic results for the proposed procedure. We next study its finite-sample properties regarding the type I error rate, the power, and the probability that the best treatment is selected for Stage 2 at the interim look. Three scenarios are considered: (1) three treatments and two stratification covariates; (2) four treatments and three stratification covariates; and (3) five treatments and two stratification covariates. We study both discrete and continuous stratification covariates. In this section, we discuss the simulation setting and results for Scenario 1. The results for Scenarios 2 and 3 and additional results showing the robustness of the proposed method to various model

misspecifications are reported in the Supplementary material.

We first consider the case of discrete stratification covariates. In Scenario 1, two experimental treatments (i.e., treatment 1 and treatment 2) are compared with one control (i.e., treatment 0) in Stage 1, and discrete stratification covariates are considered. The following linear model with two covariates Z_1 and Z_2 is used to simulate the response Y_i , for $i = 1, \dots, N + N'$,

$$Y_i = \alpha_0 + \alpha_1 T_{i1} + \alpha_2 T_{i2} + \beta_1 Z_{i1} + \beta_2 Z_{i2} + \varepsilon_i,$$

where $(\alpha_0, \alpha_1, \alpha_2, \beta_1, \beta_2)^T$ are unknown parameters; Z_1 and Z_2 follow Bernoulli distributions with success rates p_1 and p_2 , respectively; ε_i follows the normal distribution $\mathcal{N}(0, \sigma^2)$; and $T_{ik} = 1$, for $k = 1, 2$, if the i th patient is assigned to experimental treatment k , and $T_{ik} = 0$ otherwise.

In Stage 1, 120 patients sequentially enter the trial. We implement and compare the stratified permuted block design with respect to both Z_1 and Z_2 with a block size of six and complete randomization. Let

$$W_k = \frac{\bar{Y}_k - \bar{Y}_0}{(S_k^2/N_k + S_0^2/N_0)^{1/2}}, \quad k = 1, \dots, K.$$

The experimental treatment with a larger W_k , denoted as treatment k^* , is considered more effective, and is selected to continue to Stage 2. In Stage 2, 500 patients sequentially enter the trial and are randomly allocated to the control arm and treatment k^* using either a stratified permuted block design or complete randomization. At the end of the trial, we test $H_{0,k^*} : \mu_{k^*} = \mu_0$ versus $H_{1,k^*} : \mu_{k^*} > \mu_0$.

We compare four analysis approaches: (1) the traditional two-sample t -test without adjustment; (2) a linear regression with both covariates Z_1 and Z_2 in the model; (3) the bootstrap t -test proposed by Shao, Yu and Zhong (2010); and (4) our t -test with adjustment. Here, we show the bootstrap t -test for Stage 1, and it can be done similarly for Stage 2. We generate B bootstrap samples $(Y_1^{*b}, Z_{1,1}^{*b}, Z_{1,2}^{*b}), \dots, (Y_N^{*b}, Z_{N,1}^{*b}, Z_{N,2}^{*b})$, for $b = 1, 2, \dots, B$, independently by random sampling with replacement from $(Y_1, Z_{1,1}, Z_{1,2}), \dots, (Y_N, Z_{N,1}, Z_{N,2})$. We implement stratified permuted block design randomization with respect to $(Z_{1,1}^{*b}, Z_{1,2}^{*b}), \dots, (Z_{N,1}^{*b}, Z_{N,2}^{*b})$ to obtain the bootstrap analogs of treatment allocations $(T_{1k}^{*b}, \dots, T_{Nk}^{*b})$, where $T_{ik}^{*b} = 1$, for $k = 0, 1, 2$, if the i th patient is assigned to treatment k , and $T_{ik}^{*b} = 0$ otherwise. Define

Table 1. Type I error rate (percentage) in a seamless trial with three treatments and two discrete covariates.

	(p_1, p_2, σ)	Allocation	t -test	lm	BS - t	<i>Adjusted</i> - t
Simes	(0.5, 0.5, 1.0)	SPB	1.73	5.26	5.14	5.20
		CR	5.00	4.73	-	-
	(0.4, 0.6, 1.0)	SPB	1.78	4.84	5.35	5.41
		CR	4.73	4.80	-	-
	(0.4, 0.6, 1.5)	SPB	3.00	4.78	5.46	5.36
		CR	4.61	4.65	-	-
Dunnnett	(0.5, 0.5, 1.0)	SPB	1.98	5.75	5.09	5.46
		CR	5.20	5.30	-	-
	(0.4, 0.6, 1.0)	SPB	1.91	5.38	5.23	5.36
		CR	5.05	5.23	-	-
	(0.4, 0.6, 1.5)	SPB	3.38	5.27	5.17	5.40
		CR	5.09	5.08	-	-

$$\bar{Y}_k^{*b} - \bar{Y}_0^{*b} = \frac{1}{N_k^{*b}} \sum_{i=1}^N T_{ik}^{*b} Y_i^{*b} - \frac{1}{N_0^*} \sum_{i=1}^N T_{i0}^{*b} Y_i^{*b},$$

$$N_0^{*b} = \sum_{i=1}^N T_{i0}^{*b}, \quad N_k^{*b} = \sum_{i=1}^N T_{ik}^{*b}, \quad k = 1, 2.$$

The bootstrap estimator of the variance of $\bar{Y}_k - \bar{Y}_0$ is the sample variance of $\bar{Y}_k^{*b} - \bar{Y}_0^{*b}$, for $b = 1, 2, \dots, B$, denoted $\hat{\nu}_{Bj}$. The bootstrap t -test has the test statistic $T_B = (\bar{Y}_k - \bar{Y}_0) / \hat{\nu}_{Bj}^{1/2}$. We set $B = 200$ in the simulations. For the proposed t -test with adjustment, based on our theorems, the value of σ_d is estimated using Theorem 1, and the values of σ_ε and β are obtained by fitting a linear model with both covariates. The closure principle and a combination test with either the Simes or the Dunnnett test are applied to control the familywise type I error rate. The significance level α is 0.05 for all the tests. All results are based on 10,000 replications.

In Table 1, we report the type I error rate for different parameter values of (p_1, p_2, σ) , while fixing $\alpha_0 = \beta_1 = \beta_2 = 1$. Under complete randomization, the type I error rate is close to the nominal level 0.05 for both the two-sample t -test (t -test) and the full linear model (lm). Under the SPB design with either the Dunnnett or Simes test, the type I error rate of the two-sample t -test is far below 0.05, whereas our t -test with adjustment (*Adjusted*- t) successfully controls the error rate. The error is also well controlled when we use the full linear model or the bootstrap t -test (BS - t).

Table 2. Power (percentage) and number (M) of replications in which the better treatment is selected for Stage 2 in a seamless trial with three treatments and two discrete covariates.

	(α_1, α_2)	Allocation	<i>t</i> -test	<i>lm</i>	<i>BS</i> - <i>t</i>	<i>Adjusted</i> - <i>t</i>	M
Simes	(0.26, 0.16)	SPB	65.11	79.88	80.48	80.55	6,667
		CR	64.83	79.25	-	-	6,420
	(0.24, 0.16)	SPB	58.96	75.35	76.49	76.42	6,374
		CR	60.27	74.76	-	-	6,139
	(0.22, 0.16)	SPB	52.69	70.23	71.61	71.33	6,042
		CR	55.07	69.79	-	-	5,837
Dunnett	(0.26, 0.16)	SPB	65.74	80.61	80.86	80.97	6,667
		CR	65.98	80.13	-	-	6,420
	(0.24, 0.16)	SPB	60.08	76.30	77.20	77.00	6,374
		CR	61.44	75.82	-	-	6,139
	(0.22, 0.16)	SPB	53.57	71.18	72.39	72.10	6,042
		CR	56.28	71.09	-	-	5,837

In Table 2, we compare the power of the different designs and analysis approaches. We report the results for different values of (α_1, α_2) while fixing $(p_1, p_2, \sigma) = (0.5, 0.5, 1)$ and $\alpha_0 = \beta_1 = \beta_2 = 1$. Our *t*-test with adjustment and the bootstrap *t*-test under CAR have significantly higher power than the *t*-test without adjustment under either CAR or complete randomization. In addition, our design performs better than complete randomization in terms of the number of replications (M) in which the better treatment is selected for Stage 2. To save space, we present additional results for Tables 2 and 4 in the Supplementary Material.

We also performed numerical studies in which some of the covariates are continuous. To save space, we report the results for three treatments and two stratification covariates only. The setting is as in Scenario 1, except that we assume Z_2 follows a standard normal distribution. When implementing the stratified permuted block design, we discretize Z_2 into the Bernoulli variable $D(Z_2)$ as follows: $D(Z_2) = 1$ if $Z_2 < z_q$, and $D(Z_2) = 0$ otherwise, where z_q is the q th quantile of the standard normal distribution. The continuous covariate is used in the statistical inference procedures. Our *t*-test with adjustment controls the type I error at around 0.05, while the two-sample *t*-test is too conservative under the SPB design with either the Dunnett or the Simes test (Table 3). At the same time, the *t*-test with adjustment is much more powerful than the two-sample *t*-test under both the stratified permuted block design and complete randomization (Table 4).

Table 3. Type I error rate (percentage) in a seamless trial with three treatments, one discrete covariate, and one continuous covariate.

	(p_1, q, σ^2)	Allocation	<i>t-test</i>	<i>lm</i>	<i>BS-t</i>	<i>Adjusted-t</i>
Simes	(0.5, 0.5, 1.0)	SPB	1.10	4.53	5.45	5.16
		CR	4.47	4.56	-	-
	(0.4, 0.6, 1.0)	SPB	1.08	4.63	5.14	5.20
		CR	4.57	4.60	-	-
	(0.4, 0.6, 1.5)	SPB	2.16	4.89	5.31	4.96
		CR	4.55	4.58	-	-
Dunnett	(0.5, 0.5, 1.0)	SPB	1.23	4.89	5.78	5.41
		CR	5.02	4.97	-	-
	(0.4, 0.6, 1.0)	SPB	1.27	4.94	5.46	5.19
		CR	5.13	4.87	-	-
	(0.4, 0.6, 1.5)	SPB	2.31	5.09	5.66	5.31
		CR	4.89	5.10	-	-

Table 4. Power (percentage) and number (M) of replications in which the better treatment is selected for Stage 2 in a seamless trial with three treatments, one discrete covariate, and one continuous covariate.

	(α_1, α_2)	Allocation	<i>t-test</i>	<i>lm</i>	<i>BS-t</i>	<i>Adjusted-t</i>	M
Simes	(0.26, 0.16)	SPB	46.76	79.90	69.52	69.61	6,547
		CR	49.92	79.16	-	-	6,154
	(0.24, 0.16)	SPB	40.55	75.70	64.68	64.97	6,243
		CR	45.60	74.73	-	-	5,970
	(0.22, 0.16)	SPB	35.35	70.98	60.07	59.83	5,944
		CR	41.69	70.32	-	-	5,709
Dunnett	(0.26, 0.16)	SPB	48.14	80.49	70.19	70.18	6,547
		CR	51.38	79.77	-	-	6,154
	(0.24, 0.16)	SPB	41.79	76.43	65.67	65.87	6,243
		CR	46.87	75.79	-	-	5,970
	(0.22, 0.16)	SPB	36.79	72.06	60.77	60.68	5,944
		CR	43.15	71.29	-	-	5,709

4. Redesign of a Clinical Trial Evaluating Treatments for Chronic Obstructive Pulmonary Disease

COPD is a chronic lung inflammation disease that causes poor airflow from the lungs and long-term breathing problems. A double-blinded two-stage seamless clinical trial, known as the INHANCE trial, has been conducted to evaluate the efficacy and safety of indacaterol in the treatment of COPD. The trial used equal allocation with stratification for smoking status (Barnes et al. (2010));

Donohue et al. (2010)). In Stage 1, 770 patients were enrolled and four doses of indacaterol were compared with a placebo and with two active controls, formoterol and tiotropium. In Stage 2, two doses of indacaterol were selected for comparisons with a placebo and tiotropium in 1,683 patients.

Here, we redesign the INHANCE trial and evaluate the differences of trough forced expiratory volume in one second (FEV1) between multiple doses of indacaterol and the placebo. Trough FEV1 is a standard measurement of lung capacity, where a lower FEV1 indicates more severe COPD. We simplify the treatment arms into the placebo and four dose levels of indacaterol in Stage 1, and select only one dose level along with the placebo to go forward to Stage 2, following the selection rule described in the previous section. We use summary statistics for the patients and the effect sizes of the dosages in the study to create a synthetic data set of patients. To do so, we simulate the outcome FEV1 and the covariate in 112 patients in Stage 1 and 167 patients in Stage 2 using the following linear regression model:

$$Y_i = 0.15 + 0.15T_{i1} + 0.18T_{i2} + 0.22T_{i3} + 0.19T_{i4} + \beta_1 Z_{i1} + \varepsilon_i.$$

Here, $(T_{i1}, T_{i2}, T_{i3}, T_{i4})$ are indicator variables indicating the dosage assignment of the i th patient: $T_{ik} = 1$, for $k = 1, \dots, 4$, if the i th patient is assigned to dosage k , and $T_{ik} = 0$ otherwise. The binary covariate Z_{i1} indicates smoking status, with a success rate of 0.41: $Z_{i1} = 1$ if the i th patient is a current smoker, and $Z_{i1} = 0$ if the patient is an ex-smoker. Lastly, ε_i follows the normal distribution $\mathcal{N}(0, \sigma^2)$.

In both stages, a stratified permuted block design with respect to smoking status is implemented with block sizes of 10 and 6, respectively, to assign patients to different arms. In Table 5, we compare the power of the two-sample t -test and our t -test with adjustment using different values of β_1 and σ . We find that an increase in the value of the smoking status coefficient increases the power advantage of our t -test with adjustment, indicating that our t -test with adjustment is especially useful when the outcome has large differences among strata that are generated by dividing the study population using stratification covariates. We also find that a larger σ leads to a lower power for all of the tests.

5. Conclusion

Several future research directions are of interest. First, we assumed a linear model for data generation and equal allocation probabilities in order to investigate the treatment effect estimators based on the differences in the sample means

Table 5. Power (percentage) in redesigned INHANCE trial.

	(β_1, σ)	<i>t-test</i>	<i>Adjusted-t</i>		(β_1, σ)	<i>t-test</i>	<i>Adjusted-t</i>
Simes	(0.2, 0.5)	83.33	85.68	Dunnett	(0.2, 0.5)	85.20	86.92
	(0.6, 0.5)	73.22	85.72		(0.6, 0.5)	76.13	86.87
	(1.0, 0.5)	53.11	85.76		(1.0, 0.5)	56.21	86.86
	(0.2, 0.6)	69.57	72.66		(0.2, 0.6)	72.34	74.64
	(0.3, 0.6)	68.34	72.59		(0.3, 0.6)	70.97	74.49
	(0.2, 0.7)	58.07	61.22		(0.2, 0.7)	61.66	63.15
	(0.3, 0.7)	56.80	61.22		(0.3, 0.7)	60.59	63.19

under CAR. Some recent studies, however, indicate that the linearity and equal allocation assumptions may be relaxed. When there are only two arms (one treatment and one control), Ma, Tu and Liu (2020) showed that the difference-in-means estimator is unbiased and as efficient as regression-based estimators under the stratified permuted block design, even if the linear model is arbitrarily misspecified and the allocation probabilities are unequal for different arms. For the case of multiple treatments, which is more relevant to seamless trials, the theoretical properties of difference-in-means estimators have not been established, though some regression-based estimators have been studied (Bugni, Canay and Shaikh (2019)). Moreover, robust variance estimators are required for valid tests under these relaxed assumptions. The usual ordinary least squares variance estimator and Huber–White sandwich estimator are valid in a two-arm trial with equal allocation. However, in general, especially for unequal allocation, model-based variance estimators tend to fail, and consistent nonparametric estimators are preferred (Bugni, Canay and Shaikh (2018); Ma, Tu and Liu (2020)).

Second, estimation is often an important, but secondary target for seamless phase II/III trials (Posch et al. (2005); Bowden and Glimm (2014)). We have focused on hypothesis testing, the primary concern in seamless trials and another element of statistical inference. It would be interesting to explore the bias in the estimation following our design.

Third, Stallard and Friede (2008) investigated scenarios where more than one experimental treatment continues beyond the interim analysis, and sequential monitoring is implemented in Stage 2. Magirr, Jaki and Whitehead (2012) proposed methods for any number of treatment arms, stages, and patients per treatment per stage in such trials. Investigating these scenarios, especially group sequential monitoring at phase III, will be of particular interest to practitioners.

Fourth, works on seamless phase II/III designs and adaptive randomization under the Bayesian framework include, but are not limited to those of

Huang et al. (2009), Yuan, Huang and Liu (2011), Inoue, Thall and Berry (2002), Berry (2012), and Zang and Lee (2014). These designs provided insight into our study.

Fifth, seamless phase II/III designs with different study endpoints in the two stages have been investigated (Huang et al. (2009)). These have profound implications for real trials with a primary endpoint that is observed only after a long-term follow-up. It is necessary to select the treatment at the interim look based on correlated short-term endpoint data. Implementing our design in this scenario will broaden its application in practice. We leave these topics to future work.

Supplementary Material

The online Supplementary Material contains the proof of the main theorem and additional simulation results.

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