

**INTERVAL ESTIMATION FOR OPERATING
CHARACTERISTIC OF CONTINUOUS BIOMARKERS
WITH CONTROLLED SENSITIVITY OR SPECIFICITY**

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Supplementary Material

Additional simulations, with unequal case and control sizes, were conducted; other features of the setups were the same as those in the main paper. For the single-biomarker evaluation, Figures S.1 and S.2 show the results when $n_{\bullet} = n_o/2$, whereas Figures S.3 and S.4 pertain to the situations with $n_{\bullet} = n_o \times 2$. Both sets are counterparts of Figures 1 and 2 in the main paper. For the two-biomarker comparison, Table S.1 reports situations with both $n_{\bullet} = n_o/2$ and $n_{\bullet} = n_o \times 2$, in parallel to Table 1 in the main paper.

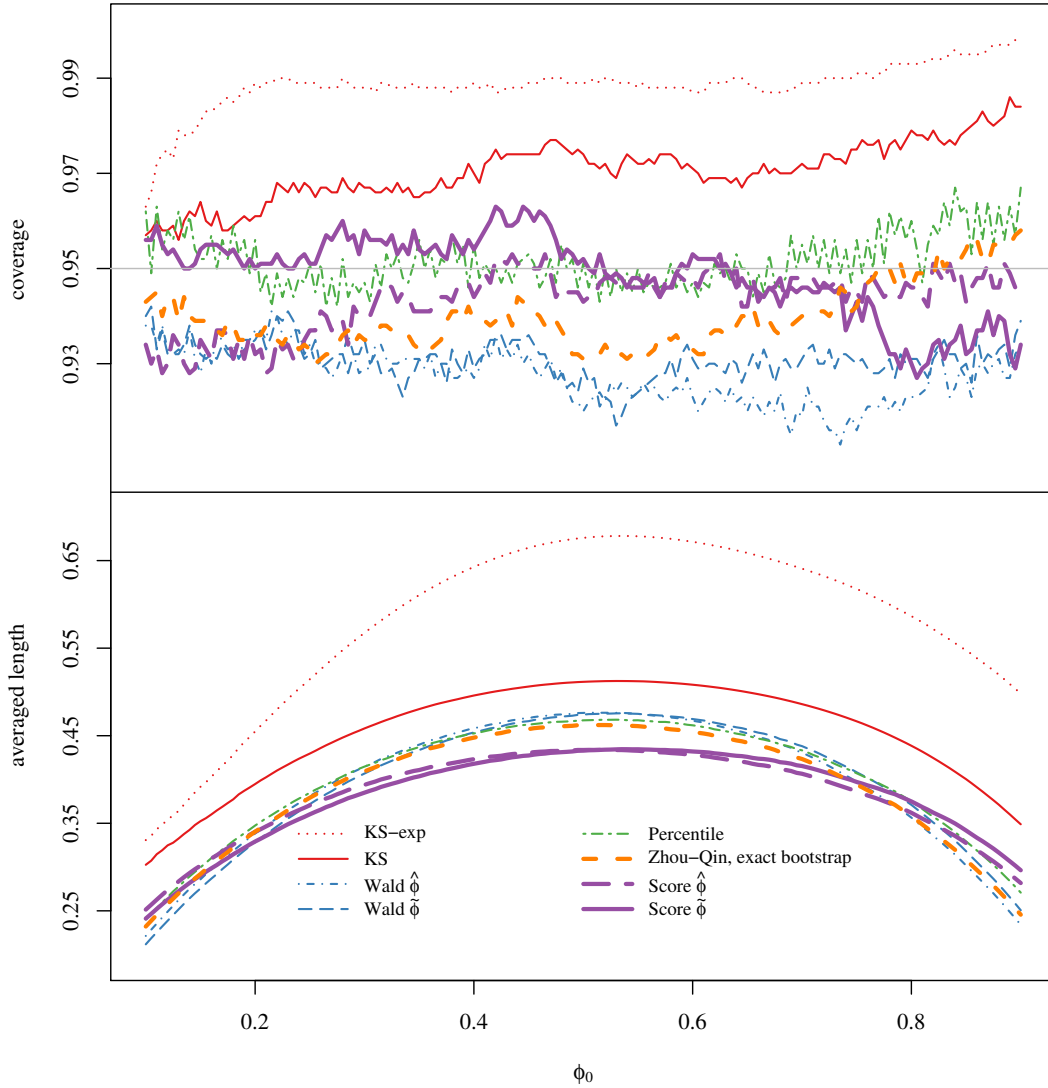


Figure S.1: Simulation summaries of 95% confidence intervals for specificity at controlled 95% sensitivity in the single-biomarker evaluation, under fixed sizes, $n_{\bullet} = 50$ and $n_{\circ} = 100$, and variable ϕ_0 . KS is the kernel smoothing-based Wald confidence intervals, as in Pepe (2003), whereas KS-exp corresponds to the KS applied to exponentially transformed biomarker data.

INTERVAL ESTIMATION FOR PERFORMANCE OF CONTINUOUS BIOMARKERS

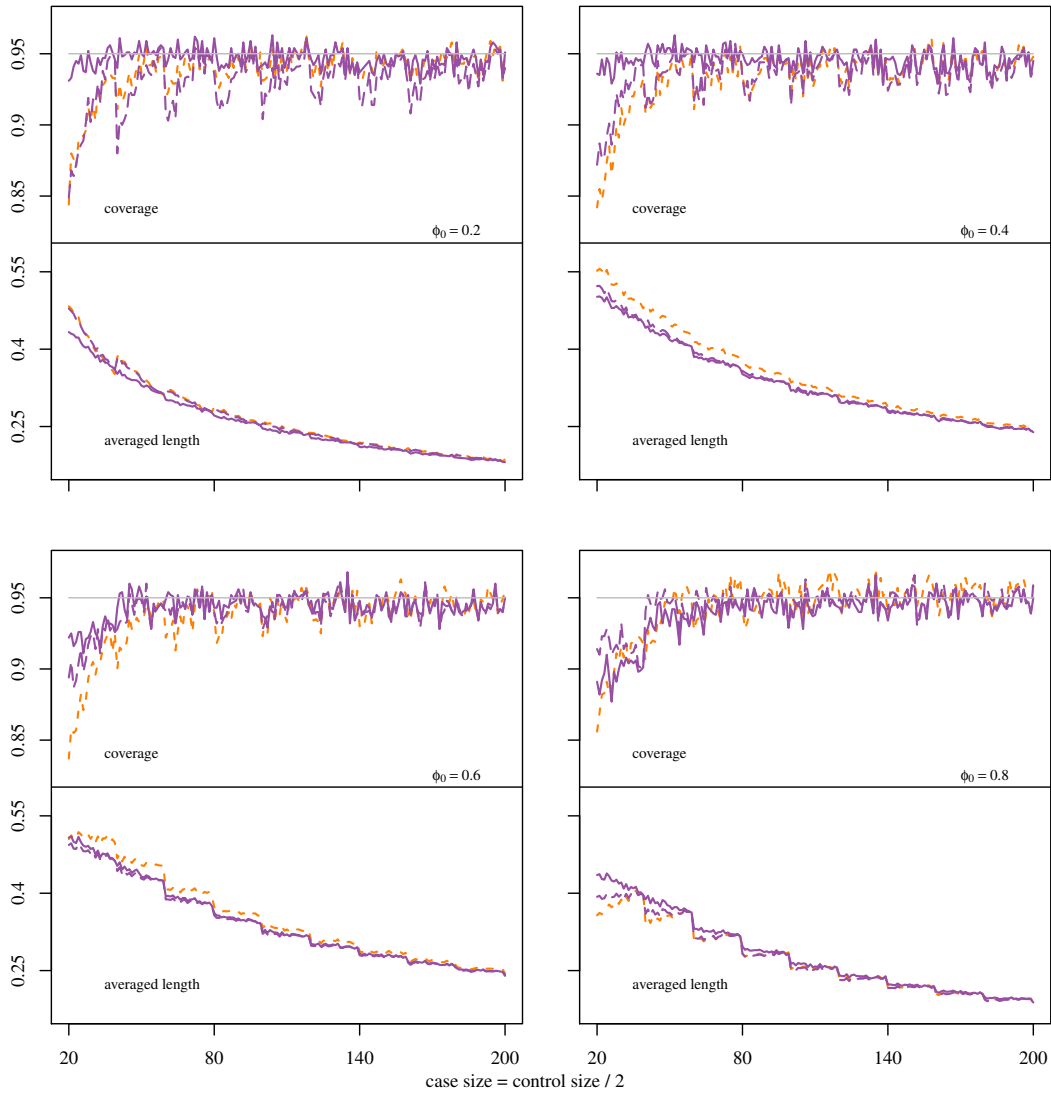


Figure S.2: Simulation summaries of 95% confidence intervals for specificity at controlled 95% sensitivity in the single-biomarker evaluation, under fixed ϕ_0 and variable sizes $n_{\bullet} = n_o/2$. Score intervals, based on $\hat{\phi}$ and $\tilde{\phi}$, and the exact bootstrap-based Zhou–Qin are included, with the same labeling as in Figure S.1.

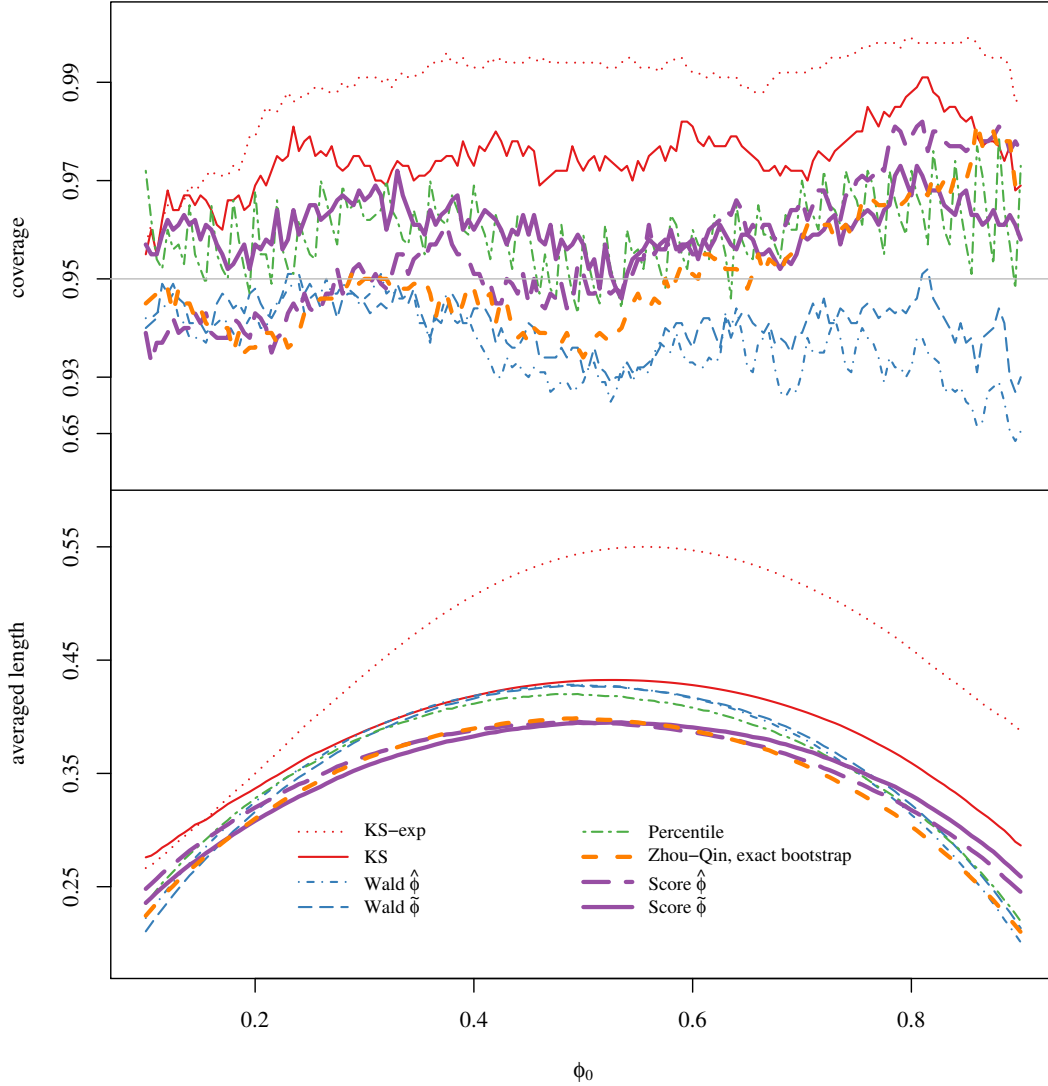


Figure S.3: Simulation summaries of 95% confidence intervals for specificity at controlled 95% sensitivity in the single-biomarker evaluation, under fixed sizes, $n_{\bullet} = 100$ and $n_{\circ} = 50$, and variable ϕ_0 . KS is the kernel smoothing-based Wald confidence intervals, as in Pepe (2003), whereas KS-exp corresponds to the KS applied to exponentially transformed biomarker data.

INTERVAL ESTIMATION FOR PERFORMANCE OF CONTINUOUS BIOMARKERS

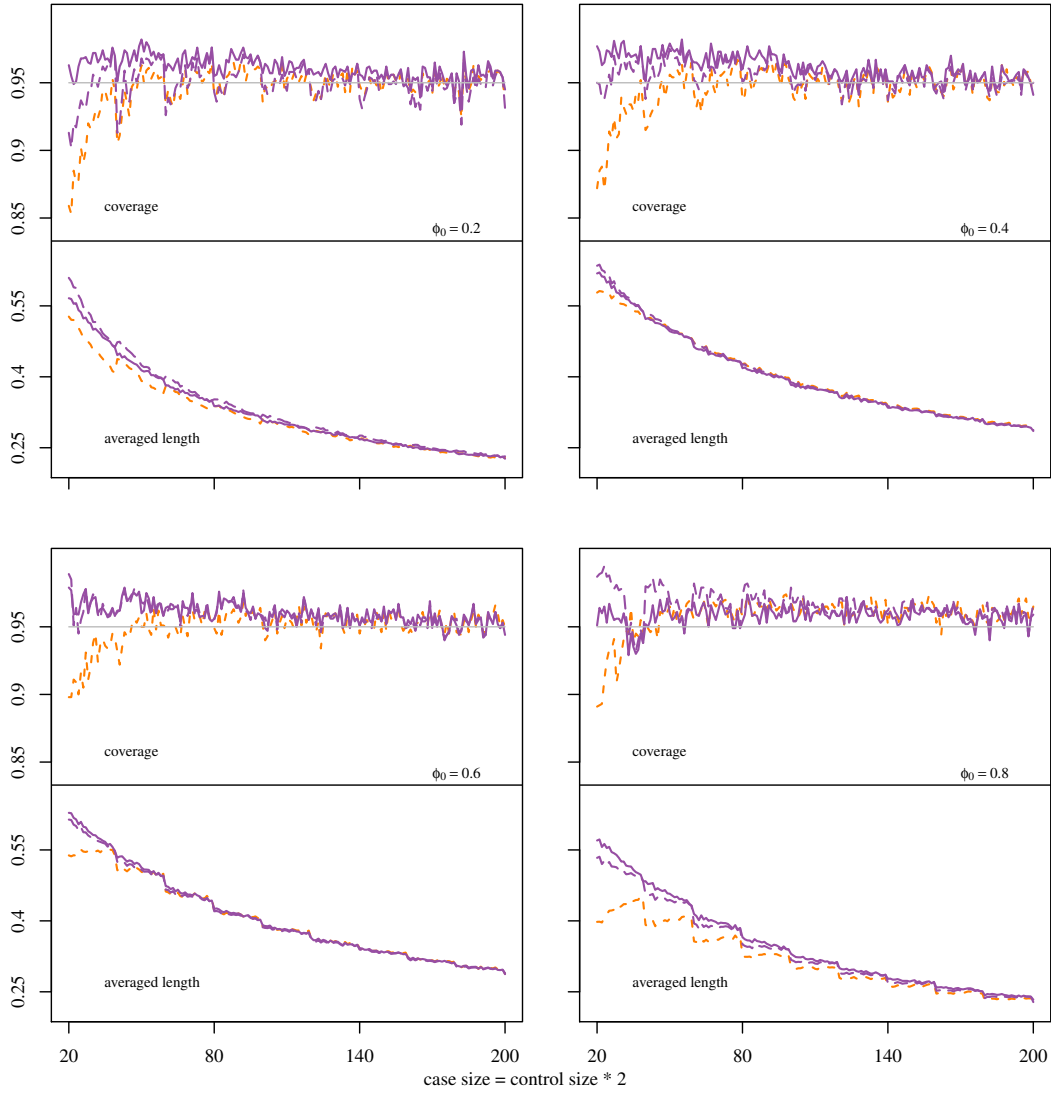


Figure S.4: Simulation summaries of 95% confidence intervals for specificity at controlled 95% sensitivity in the single-biomarker evaluation, under fixed ϕ_0 and variable sizes $n_{\bullet} = n_o \times 2$. Score intervals, based on $\hat{\phi}$ and $\tilde{\phi}$, and the exact bootstrap-based Zhou–Qin are included, with the same labeling as in Figure S.3.

Table S.1: Simulation summary statistics of exact bootstrap-based 95% confidence intervals for difference in specificity at controlled 95% sensitivity in the two-biomarker comparison.

| ϕ_{0X} | δ_0 | n_{\bullet}/n_{\circ} | | unpaired biomarkers | | | | | paired biomarkers | | | | | |
|-------------|------------|-------------------------|--------|---------------------|----------------|-----|--------------|----------------|-------------------|----------------|-----|--------------|----------------|-----|
| | | | | Wald | | Pct | Score | | Wald | | Pct | Score | | |
| | | | | $\hat{\phi}$ | $\tilde{\phi}$ | | $\hat{\phi}$ | $\tilde{\phi}$ | $\hat{\phi}$ | $\tilde{\phi}$ | | $\hat{\phi}$ | $\tilde{\phi}$ | |
| 0.2 | 0.0 | 75/150 | C | 960 | 967 | 977 | 962 | 968 | 964 | 971 | 985 | 967 | 975 | |
| | | | L | 431 | 431 | 427 | 375 | 370 | 387 | 387 | 384 | 344 | 339 | |
| | | 150/75 | C | 960 | 967 | 981 | 962 | 964 | 959 | 959 | 984 | 963 | 962 | |
| | | | L | 387 | 387 | 386 | 347 | 342 | 344 | 344 | 344 | 315 | 310 | |
| 0.4 | 0.2 | 75/150 | C | 946 | 951 | 975 | 947 | 950 | 953 | 956 | 980 | 955 | 960 | |
| | | | L | 510 | 510 | 502 | 443 | 439 | 460 | 460 | 453 | 409 | 405 | |
| | | 150/75 | C | 963 | 963 | 978 | 959 | 958 | 963 | 970 | 984 | 969 | 970 | |
| | | | L | 449 | 449 | 447 | 403 | 400 | 401 | 401 | 399 | 367 | 364 | |
| | 0.0 | 75/150 | C | 948 | 950 | 972 | 951 | 956 | 954 | 958 | 987 | 958 | 960 | |
| | | | L | 576 | 576 | 568 | 495 | 492 | 519 | 519 | 511 | 457 | 455 | |
| | | 150/75 | C | 962 | 965 | 982 | 963 | 965 | 961 | 959 | 984 | 961 | 960 | |
| | | | L | 502 | 502 | 500 | 447 | 445 | 444 | 444 | 443 | 405 | 403 | |
| 0.6 | 0.4 | 75/150 | C | 950 | 953 | 975 | 944 | 944 | 955 | 958 | 979 | 943 | 951 | |
| | | | L | 521 | 521 | 509 | 459 | 458 | 473 | 474 | 461 | 426 | 425 | |
| | | 150/75 | C | 949 | 950 | 976 | 950 | 950 | 961 | 965 | 987 | 957 | 960 | |
| | | | L | 448 | 448 | 445 | 408 | 407 | 404 | 404 | 402 | 375 | 374 | |
| | 0.2 | 75/150 | C | 954 | 952 | 970 | 956 | 959 | 955 | 961 | 986 | 959 | 959 | |
| | | | L | 586 | 586 | 576 | 505 | 505 | 530 | 530 | 518 | 468 | 468 | |
| | | 150/75 | C | 953 | 953 | 976 | 951 | 952 | 958 | 960 | 984 | 960 | 956 | |
| | | | L | 501 | 501 | 500 | 448 | 448 | 446 | 446 | 444 | 407 | 407 | |
| | 0.0 | 75/150 | C | 954 | 953 | 974 | 953 | 956 | 968 | 972 | 984 | 970 | 971 | |
| | | | L | 597 | 597 | 584 | 511 | 513 | 539 | 539 | 526 | 473 | 476 | |
| | | 150/75 | C | 957 | 951 | 979 | 956 | 951 | 965 | 966 | 983 | 962 | 965 | |
| | | | L | 503 | 503 | 501 | 448 | 450 | 445 | 445 | 443 | 405 | 408 | |
| | 0.8 | 0.6 | 75/150 | C | 956 | 955 | 969 | 931 | 933 | 960 | 962 | 978 | 937 | 935 |
| | | | | L | 457 | 458 | 447 | 421 | 422 | 418 | 419 | 407 | 391 | 391 |
| | | | 150/75 | C | 942 | 949 | 977 | 955 | 946 | 960 | 965 | 982 | 938 | 942 |
| | | | | L | 389 | 389 | 387 | 368 | 368 | 357 | 357 | 355 | 340 | 341 |
| 0.4 | | 75/150 | C | 966 | 967 | 969 | 943 | 945 | 965 | 968 | 980 | 942 | 947 | |
| | | | L | 531 | 532 | 519 | 469 | 470 | 485 | 485 | 473 | 436 | 438 | |
| | | 150/75 | C | 961 | 957 | 974 | 960 | 964 | 955 | 949 | 986 | 940 | 949 | |
| | | | L | 450 | 450 | 448 | 409 | 411 | 407 | 407 | 405 | 377 | 378 | |
| 0.2 | | 75/150 | C | 961 | 959 | 964 | 952 | 953 | 966 | 970 | 979 | 959 | 962 | |
| | | | L | 543 | 543 | 528 | 469 | 473 | 494 | 494 | 478 | 437 | 441 | |
| | | 150/75 | C | 957 | 959 | 972 | 954 | 951 | 967 | 962 | 992 | 956 | 962 | |
| | | | L | 451 | 451 | 450 | 405 | 409 | 404 | 404 | 403 | 370 | 374 | |
| 0.0 | 75/150 | C | 969 | 966 | 976 | 963 | 964 | 968 | 970 | 981 | 964 | 966 | | |
| | | L | 488 | 488 | 469 | 420 | 427 | 438 | 438 | 422 | 387 | 393 | | |
| | 150/75 | C | 966 | 962 | 986 | 966 | 964 | 976 | 974 | 992 | 978 | 972 | | |
| | | L | 395 | 395 | 395 | 353 | 360 | 352 | 352 | 353 | 321 | 327 | | |

For unpaired comparison, $n_{\bullet X} = n_{\bullet Y}$ and $n_{\circ X} = n_{\circ Y}$ were set to n_{\bullet} and n_{\circ} , respectively.
 C: coverage probability ($\times 1000$); L: average interval length ($\times 1000$). Pct: percentile interval.