

## Foreword

This is a special issue in honor of Professor David Siegmund's 70th birthday. It consists of 17 papers in the areas of *Statistical genetics*, *Change-point problems*, *Random fields*, and *Sequential analysis*. They represent the major areas of the research of Professor Siegmund, who has made seminal contributions, with far-ranging impacts, to these areas, which will be reviewed below. Some of the papers are expanded versions of talks presented in June 2011 at the Third International Workshop on Sequential Methodologies (IWSM3) and the Conference on Genetics, Probability, and Statistics (GPS), held in honor of his 70th birthday (<http://statistics.stanford.edu/gps>).

### Statistical genetics

The monograph by Siegmund and Yakir (2007) gives an elegant and lucid overview of the statistical methods and problems in identifying, or mapping, the genes associated with certain phenotypes, or traits. The book covers many important topics in experimental and human genetics, together with related models and statistical methods, including significance level and power of genome scans, confidence bounds for the genetic effects of quantitative trait loci (QTL), model selection in mapping QTL, and multipoint linkage analysis, to which Professor Siegmund and his coauthors have made fundamental contributions; see for example Feingold, Brown, and Siegmund (1993), Dupuis, Brown, and Siegmund (1995), Dupuis and Siegmund (1999), Teng and Siegmund (1998), Tang and Siegmund (2002), Siegmund and Yakir (2003), Siegmund (2004), Peng and Siegmund (2004), and Peng, Tang, and Siegmund (2005). Recent major advances by Professor Siegmund's group include mapping quantitative traits for unselected families in Dupuis et al. (2009), and statistical methods for detecting copy number variations; see Siegmund, Yakir, and Zhang (2011a), and Zhang et al. (2010).

The first four papers in this special issue are in the area of statistical genetics. The fifth, by Chen, Fang, and Shao, is on Poisson approximations for dependent trials, which have applications in genomic sequence analysis, as first noted by Arratia, Gordon, and Waterman (1990).

### Change-point problems

Siegmund (2013) has pointed out the close connection between the statistical methodologies for genome scans and change-point problems. In particular, he

notes that whereas change-point methodology had its origins in sequential detection of a change-point, as in quality control charts, “applications in biology and, more specifically, genetics” have motivated change-point problems in fixed samples, which “are now completing the circle back to sequential detection, now involving complex signals arising from multiple sources and/or detection by multiple sensors.” Professor Siegmund has made fundamental contributions to both sequential and fixed-sample change-point problems; see for example Siegmund (1988), Siegmund and Venkatraman (1995), Siegmund and Worsley (1995), Rabinowitz and Siegmund (1997), Tu and Siegmund (1999), Siegmund and Yakir (2000), Siegmund, Zhang, and Yakir (2011b), and Xie and Siegmund (2013).

In this special issue, Tu’s paper introduces a ratchet scan statistic whose scanning window is a grid instead of a rectangular box, to detect cosmic ray pion particles in high energy physics. The paper by Hao, Niu and Zhang develops a novel false discovery rate approach to multiple change-point detection and applies it to the analysis of copy number variations. An alternative approach to multiple change-points using empirical Bayes (EB) filters and smoothers in hidden Markov models (HMM) is used in the paper by Lai and Xing to develop stochastic change-point models with contemporaneous jumps in regression parameters and long-run volatilities for econometric time series. The paper by Dicker, Sun, Zhang, Keenan, and Shepp synthesizes ideas from HMM, filtering, sequential change-point detection algorithms for real-time estimation of blood glucose density from sensor measurements in continuous glucose monitoring systems for managing diabetes.

### **Random fields**

Scan statistics are closely related to the maxima of random fields. While they represent one direction of Siegmund’s work in random fields, another direction was undertaken by him earlier in connection with inference in nonlinear regression models using the Hotelling–Weyl formula for the volumes of tubes around smooth curves and more general manifolds; see Johnstone and Siegmund (1989), Knowles and Siegmund (1989), and Siegmund and Zhang (1993). The papers by Taylor and Worsley, Yakir, and Wang and Woodroffe in this special issue are in the area of random fields.

### **Sequential analysis**

The last five papers in this special issue belong to the area of sequential analysis and related boundary crossing problems, which was the focus of Professor Siegmund’s research from his graduate student days at Columbia University to the time when he finished his influential monograph on the subject in 1985. Another

book he published in this area, with Chow and Robbins in 1971, is related to his Ph.D. thesis on optimal stopping. Some of Professor Siegmund's seminal contributions in this area can be found from these two books and in Sections 2.2 and 2.3 of Lai (2009).

On behalf of the Organizing Committees of GPS and IWSM3, I want to thank *Statistica Sinica* for publishing this special issue and to express my appreciation to the Co-Editor, Professor Qiwei Yao, for his excellent and timely editorial work. We would like to use this opportunity to congratulate Professor Siegmund on his achievements and wish him many more happy and productive years.

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