## Corrections on

## SOME INSIGHTS ABOUT THE SMALL BALL PROBABILITY FACTORIZATION FOR HILBERT RANDOM ELEMENTS

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1. In defining the residual term  $\mathcal{R}(x,\varepsilon,d)$  in equation (3.1) (and (3.5) in the Supplementary materials), the mean is conditioned to  $(x_1,\ldots,x_d)$  as follows:

$$\mathcal{R}(x,\varepsilon,d) = \mathbb{E}\left[ (1-S)^{d/2} \mathbb{I}_{\{S\leq 1\}} \middle| (x_1,\ldots,x_d) \right].$$

This new definition leaves true all the remaining statements in the paper; in particular, the min–max Courant–Fisher principle guarantees that Lemma 1 (in the Supplementary Materials) and Proposition 1 hold true.

- 2. In the proof of Theorem 1 (in the Supplementary materials), the following modifications have to been made:
  - The density  $f_d(\cdot)$  which appears at the top of page 2 (in lines 1, 3 and 6) is the conditional density  $f_{d|s}(\cdot)$  to S=s;
  - The first two equations at the top of page 3 have to be modified as follows:

$$\left| \frac{\int_{0}^{1} \left( \varphi(s|x,\varepsilon,d) - f(x_{1},\ldots,x_{d})I \right) dG\left(s\right)}{\int_{0}^{1} f(x_{1},\ldots,x_{d})I dG\left(s\right)} \right| \leq$$

$$\leq \left| \frac{\frac{\varepsilon^{2}}{2\lambda_{d}}C_{2} \int_{0}^{1} f(x_{1},\ldots,x_{d})I dG\left(s\right)}{\int_{0}^{1} f(x_{1},\ldots,x_{d})I dG\left(s\right)} \right| = C_{2} \frac{\varepsilon^{2}}{2\lambda_{d}}$$

and, supposing that S has positive density over (0,1),

$$\int_0^1 f_{d|s}(x_1, \dots, x_d) I(s, \varepsilon, d) dG(s) = f_d(x_1, \dots, x_d) \int_0^1 I(s, \varepsilon, d) f_{S|d}(s) ds$$
$$= \frac{\varepsilon^d \pi^{d/2}}{\Gamma(d/2+1)} \mathbb{E} \left[ (1-S)^{d/2} \mathbb{I}_{\{S \le 1\}} \middle| (x_1, \dots, x_d) \right]$$

where  $f_{S|d}(s)$  is the conditional density of S to  $(\theta_1, \dots, \theta_d) = (x_1, \dots, x_d)$ .

3. The right hand side of Equation (5.3) must be multiplied by 2.