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CORRECTION: Derivative principal components for representing the time dynamics of longitudinal and functional data

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Abstract: We provide corrections to Dai, X., Tao, W., Müller, H.G. (2018).

Derivative principal components for representing the time dynamics of longitudinal and functional data in the rates of convergence of the local polynomial estimates of the derivative mean and the covariance functions.

Key words and phrases: Derivatives, Empirical dynamics, Functional principal component analysis, Growth curves, Best linear unbiased prediction.

We are grateful to Dr. Hassan Sharghi (Shahid Beheshti University) for pointing out some errors in this paper, for which we provide corrections in the following.

The definitions of a_n in (4.1)–(4.2) missed some factors h_μ and h_G in the denominators. The corrected version is as follows:

$$a_{n1} = h_\mu^2 + \sqrt{\frac{\log(n)}{nh_\mu^3}}, \quad b_{n1} = h_G^2 + \sqrt{\frac{\log(n)}{nh_G^6}}, \quad (4.1)$$

$$a_{n2} = h_\mu^2 + \sqrt{\left(1 + \frac{1}{mh_\mu}\right) \frac{\log(n)}{nh_\mu^2}}, \quad b_{n2} = h_G^2 + \left(1 + \frac{1}{mh_G}\right) \sqrt{\frac{\log(n)}{nh_G^4}}. \quad (4.2)$$

As a result, conditions (A5) and (A7) change

$$(A5) \quad h_\mu \rightarrow 0 \text{ and } \log(n) \sum_{i=1}^n N_i w_i^2 / h_\mu^3 \rightarrow 0, \log(n) \sum_{i=1}^n N_i (N_i - 1) w_i^2 / h_\mu^2 \rightarrow 0.$$

$$(A7) \quad h_G \rightarrow 0, \log(n) \sum_{i=1}^n N_i (N_i - 1) v_i^2 / h_G^6 \rightarrow 0, \log(n) \sum_{i=1}^n N_i (N_i - 1) (N_i - 2) (N_i - 3) v_i^2 / h_G^4 \rightarrow 0.$$

In the first paragraph after Theorem 1, the optimal rate of convergence for $\hat{G}^{(1,1)}$ and $\hat{\phi}_{k,1}$ should be $O((\log(n)/n)^{1/5})$, almost surely, achieved, for example, if $h_\mu \asymp (\log(n)/n)^{1/7}$, $h_G \asymp (\log(n)/n)^{1/10}$, $\alpha > 14/5$, and $\beta > 10/3$, as in (A6) and (A8). In the dense case, the root- n rate can no longer be achieved because of the variance term b_{n2} .

In the proof of Theorem 1, for $h_\mu \hat{\mu}^{(1)}(t) = h_\mu \hat{\alpha}_1 = |\mathbf{S}|^{-1}(C_{12}R_0 + C_{22}R_1 + C_{32}R_2)$, the cofactors of $[\mathbf{S}]_{1,2}$, $[\mathbf{S}]_{2,2}$, and $[\mathbf{S}]_{3,2}$ should instead be defined as

$$C_{12} = - \begin{vmatrix} S_1 & S_3 \\ S_2 & S_4 \end{vmatrix}, \quad C_{22} = \begin{vmatrix} S_0 & S_2 \\ S_2 & S_4 \end{vmatrix}, \quad C_{23} = - \begin{vmatrix} S_0 & S_2 \\ S_1 & S_3 \end{vmatrix},$$

respectively. The second-order terms in the Taylor expansion of $h_\mu(\hat{\alpha}_1 - \mu^{(1)}(t))$ should be divided by an additional factor of 2. The asymptotic variance terms in the last equation on page 1604 and the first expression on page 1605 should be divided by an additional factor of h_μ .

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